

## New Calibrations for Determining Soil Electrical Conductivity—Depth Relations from Electromagnetic Measurements

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### ABSTRACT

Soil salinity can be determined in the field from measurements of soil electrical conductivity ( $EC_a$ ). Measurements of depth-integrated  $EC_a$  can be made remotely using electromagnetic induction (EM) techniques. A means of determining  $EC_a$  for the soil depth intervals of 0 to 30, 30 to 60, 60 to 90 cm, etc., from the EM measurements is needed for salinity appraisal. The EM and  $EC_a$  measurements were made at about 900 sites in the San Joaquin Valley of California. This large data set was used, along with rigorous statistical techniques, to obtain empirical coefficients used in equations to predict  $EC_a$  by depth intervals within the soil profile from EM readings taken above ground. Predictions were found to be more accurate using these new coefficients rather than those previously available.

**A** DEPTH-WEIGHTED VALUE of soil electrical conductivity, can be determined from above-ground EM measurements through a depth which depends on the coil orientation, the spacing between transmitter and receiver coils, and the electrical frequency of the

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instrument. Rhoades and Corwin (1981) demonstrated that bulk soil  $EC_a$ , within discrete depth intervals of the soil profile could be determined from EM readings made at a succession of heights above the ground (e.g., 0, 30, 60, 90, and 120 cm) by solving a set of empirical equations containing depth-specific coefficients. The values of the coefficients utilized in these equations were determined by multiple linear regression analysis of successive EM readings measured with a Geonics EM-38<sup>1</sup> device (Geonics Limited, Mississauga, Ontario, Can.), and of corresponding  $EC_a$  values for the soil-depth intervals of 0 to 30, 30 to 60, 60 to 90 and 90 to 120 cm measured using a Martek SCT<sup>1</sup> (Martek Instruments, Inc., Irvine, CA) four-electrode probe (Rhoades and van Schilfgaarde, 1976).

A simpler and almost as accurate method was later developed to determine the distribution of  $EC_a$  within the soil profile using only two EM measurements taken at the soil surface with the long axis of the EM-38 device's electromagnet oriented parallel ( $EM_H$ ) and then perpendicular ( $EM_V$ ) to the soil surface (Corwin and Rhoades, 1982). Equations containing depth-spe-

<sup>1</sup> Product identification is provided solely for the benefit of the reader and does not imply the endorsement of the USDA.

cific coefficients were developed relating  $EC_a$  within specific soil-depth intervals to  $EM_H$  and  $EM_V$ .

Corwin and Rhoades (1983) later found that different coefficients were needed in the equations relating  $EC_a$  to  $EM_H$  and  $EM_V$  for soils in which  $EC_a$  decreased with depth, i.e., inverted salinity profiles, compared to soils in which  $EC_a$  increased with depth, i.e., normal salinity profiles. The data sets for these coefficients were quite limited. This paper presents new coefficients obtained from a more extensive data base using statistical techniques which account for the existence of collinearity between  $EM_H$  and  $EM_V$  measurements.

### THEORY

Corwin and Rhoades (1982) related  $EC_a$  within a given depth interval,  $EC_{a,x_1-x_2}$ , to  $EM_H$  and  $EM_V$  by the equation

$$EC_{a,x_1-x_2} = k_1 EM'_H - k_2 EM''_H - k_3 EM_V, \quad [1]$$

where  $EM'_H$  and  $EM''_H$  are adjusted values of  $EM_H$  (obtained empirically) and the values of  $k_1$ ,  $k_2$  and  $k_3$  are depth-specific, empirically determined coefficients.

Substituting the appropriate equations describing  $EM_H$  and  $EM_V$  as functions of  $EM_H$  into Eq. [1] yields the equivalent relation

$$EC_{a,x_1-x_2} = k_H EM_H - k_V EM_V + k, \quad [2]$$

where  $k_H$ ,  $k_V$  and  $k$  are empirically determined coefficients for the depth interval  $x_1-x_2$ . The value  $k$  should ideally be zero, but often is not, due to experimental error or "noise" in the data which disallows a perfect fit of the  $EM-EC_a$  relations. In the results that follow,  $k$  was retained in the expression if it was significantly different from zero; otherwise zero-intercept regression techniques were used.

### EXPERIMENTAL PROCEDURE

The  $EM_H$  and  $EM_V$  were measured using the Geonics EM-38 device at 900 sites within a 39-km<sup>2</sup> area of the South Kings River Watershed of the San Joaquin Valley of California (representing at least 10 different soil types varying in texture from loamy sand to clay). At each site, corresponding values of  $EC_a$  were measured using the Martek SCT insertion probe for the intervals 0 to 30 and 30 to 60 cm; at every third site  $EC_a$  was also measured for the interval 60 to 90 cm. The  $EC_a$  was also measured at each site using an array of electrodes inserted into the soil surface in the Wenner configuration (see Rhoades, 1976). Inner-electrode spacings of both 30 and 60 cm were used in these measurements. The  $EC_a$  values for the 0 to 30-, 0 to 60-, and 30 to 60-cm intervals were estimated from the Wenner array measurements (Rhoades, 1976; Rhoades and van Schilfgaarde, 1976).

Exploratory data analysis techniques (Tukey, 1977) were used to determine the frequency distributions of the measured  $EM$  and  $EC_a$  data. The data were transformed in order to obtain normal distributions so that valid statistical analyses could be performed. This was necessary because the distributions of each parameter were highly skewed with a preponderance of low values and a substantially smaller number of high values. Three transformations were tried: natural log, square root and fourth root. As revealed by the Shapiro-Wilk test statistic (Shapiro and Wilk, 1965), the fourth-root transformation normalized all of the variables; consequently, all subsequent statistics were applied to fourth-root transformed data. Hereafter, the symbol  $\hat{\phantom{x}}$  will be used to denote parameters which have been raised to the one-fourth power.

The normalized data set ( $n = 900$  samples) was randomly split into two subsets, so that one set could be used to estimate the parameters  $k_H$ ,  $k_V$  and  $k$  and the other to test the validity of Eq. [2] and the determined coefficients. Additionally, within each subset the  $EM_H$  and  $EM_V$  values were split by salinity profile condition (inverted or normal). Inverted profiles were those where  $EM_H > EM_V$  and  $EM_H/EM_V > 1.05$ ; normal profiles were those where  $EM_H \leq EM_V$ .

Regression analysis was used to solve Eq. [2] for  $k_H$  and  $k_V$ . Extreme collinearity between the  $EM_H$  and  $EM_V$  values was detected when the results of the two SCT data sets obtained using the Martek SCT probe were compared. This necessitated the use of statistical procedures which combat multicollinearity. Three techniques were evaluated for their effectiveness in obtaining stable and valid coefficients. They were: (i) ridge regression (Myers, 1986; Statgraphics, 1986), (ii) principal components analysis (Davis, 1986) and (iii) best linear combination transformation as ascertained by a SAS regression procedure (PROC REG; SAS Institute, Inc., 1985). These techniques were not applied to the two Wenner data sets because stable and valid coefficients were obtained in the regression analysis performed on these data sets.

A small set of  $EM_H$ ,  $EM_V$ , and  $EC_a$  values ( $n = 18$ ) was obtained after completion of the analysis of the major, extensive data set and used to evaluate the accuracy of the  $EC_a$  predictions made using the values of the  $k_H$  and  $k_V$  obtained from the extensive data set. These new data were acquired from within the same study area as previous samples, but this time multiple measurements of  $EM$  and  $EC_a$  were made at each of the sampled sites in order to obtain more representative readings of  $EM$  and  $EC_a$ , especially of  $EC_a$  within the soil volume measured by the EM-38 device. Eight readings of  $EM_H$  and  $EM_V$  were made at each site; the EM-38 device was read in both positions (H and V) when pointed at each of the eight cardinal compass directions. The  $EC_a$  was measured at eight locations within the 0- to 30-, 30- to 60- and 60- to 90-cm soil-depth intervals; these locations were 25 cm out from the site-center along each compass heading.

### RESULTS AND DISCUSSION

No optimal stopping criterion was found for ridge regression and the tolerance level for the matrix multiplication was insufficient; hence, it was abandoned as a method to eliminate collinearity in the Martek SCT data sets.

Since it was unclear how to account for differing soil depths in the two salinity profile conditions using principal components analysis (PC), all of the  $EM_H$  and  $EM_V$  measurements were used without distinction between soil depth or profile condition, and one overall weighting function was obtained. The result was

$$PC_{EM} = 0.4787 \hat{EM}_H + 0.5213 \hat{EM}_V. \quad [3]$$

The best linear combination method (SAS Institute, Inc., 1985) yielded six weighting functions for the entire Martek SCT data set. Each function corresponded to the appropriate soil depth and profile condition. The functions obtained for the case where  $EM_H \leq EM_V$  were

$$\text{depth 0 to 30 cm, } SAS_{EM}^{\hat{}} = 3.050 \hat{EM}_H - 2.000 \hat{EM}_V, \quad [4]$$

$$\text{depth 30 to 60 cm, } SAS_{EM}^{\hat{}} = 2.585 \hat{EM}_H - 1.213 \hat{EM}_V, \quad [5]$$

$$\text{depth 60 to 90 cm, } \text{SAS}_{EM}^{\hat{}} = 0.958 \text{EM}_H^{\hat{}} - 0.323 \text{EM}_V^{\hat{}}, \quad [6]$$

and where  $\text{EM}_H > \text{EM}_V$ , they were

$$\text{depth 0 to 30 cm, } \text{SAS}_{EM}^{\hat{}} = 0.830 \text{EM}_H^{\hat{}} - 0.640 \text{EM}_V^{\hat{}}, \quad [7]$$

$$\text{depth 30 to 60 cm, } \text{SAS}_{EM}^{\hat{}} = 0.591 \text{EM}_H^{\hat{}} + 0.635 \text{EM}_V^{\hat{}}, \quad [8]$$

$$\text{and depth 60 to 90 cm, } \text{SAS}_{EM}^{\hat{}} = -0.126 \text{EM}_H^{\hat{}} + 1.283 \text{EM}_V^{\hat{}}. \quad [9]$$

The linear-combinations (Eq. [3]–[9]) were then used in the linear regression analysis (SAS Institute, Inc., 1985) to estimate the coefficients of Eq. [2] for the random-split data sets and the results were again examined to see if parameter stability could now be achieved. In order to test for significant differences in the parameter estimates between the different splits, a categorical variable (*DS*) was introduced into these equations to identify the subset. The analogous relations to Eq. [2] then became

$$\text{EC}_{a,x_1-x_2}^{\hat{}} = B_0 + B_1 \text{PC}_{EM}^{\hat{}} + B_2 (DS), \quad [10]$$

and

$$\text{EC}_{a,x_1-x_2}^{\hat{}} = B_0 + B_1 \text{SAS}_{EM,x_1-x_2}^{\hat{}} + B_2 (DS). \quad [11]$$

If a difference existed between the two data splits, the  $B_2$  parameter would be significantly different from zero. Since the values of  $B_2$  were not significantly different from zero in any case, we concluded that stability was achieved using Eq. [10] and [11] and that the two SCT data splits were equivalent (see Table 1). Therefore these two sets of data were combined and the remainder of the analyses were performed using the total data.

Our next step was to choose between Eq. [10] and [11] for establishing the coefficients of Eq. [2] for the Martek SCT data sets. Since both are essentially linear weighting functions and all of the transformations used were scaled similarly, the models could be directly compared. The criteria used for this comparison were the  $r^2$ , and the Press statistic<sup>2</sup> (SAS Institute, Inc., 1985;

<sup>2</sup> The Press statistic is the sum of squares of the residuals calculated by taking the difference of the  $i^{\text{th}}$  observed value and the  $i^{\text{th}}$  predicted value, where the latter value is obtained from a regression equation derived from the  $i-1$  data points. Thus in choosing a best model, one selects the model with the lowest Press statistic (Myers, 1986, p. 106–111).

Table 1. Values of  $B_2$  coefficients in Eq. [10] and [11] and their  $F$  probability levels, using SCT values of  $\text{EC}_a$ .

Profile	Depth, cm	Eq. [10]		Eq. [11]	
		$B_2$	( $P_r > F$ )**	$B_2$	( $P_r > F$ )**
$\text{EM}_H \leq \text{EM}_V$	0–30	0.002	0.861	0.000	0.954
	30–60	–0.000	0.708	–0.004	0.667
	60–90	–0.021	0.261	–0.022	0.259
$\text{EM}_H > \text{EM}_V$	0–30	0.013	0.574	0.017	0.401
	30–60	–0.028	0.204	0.028	0.205
	60–90	–0.023	0.558	–0.018	0.644

\*\* Probabilities greater than 0.01 were not considered to be significantly different from zero.

Myer, 1986). The results of this analysis are given in Table 2. The SAS linear combinations (Eq. 11) gave the better fits and prediction capabilities. Furthermore, the intercept value ( $B_0$ ) was insignificant for four of the six models (Eq. [4]–[9]) and hence could be eliminated.

The SAS linear combination model was then used (since it was the better model) to calculate the coefficients of Eq. [2] (separately for each depth interval and for the two profile conditions) from the  $\text{EM}_H$ ,  $\text{EM}_V$  and  $\text{EC}_a$  readings. For this purpose, the two random-split data sets have been combined, since the values of the coefficients to be obtained would be the same for the splits and the whole set, as is evidenced in the results given in Table 1 and as discussed above. These results are given in Table 3. The relatively high  $r^2$  values show the good correspondence obtained between  $\text{EC}_a$  and  $\text{EM}_H$  and  $\text{EM}_V$ .

The relations of Table 3 were then used to predict  $\text{EC}_a$  values from given  $\text{EM}_H$  and  $\text{EM}_V$  values. The correspondence between these predicted values of  $\text{EC}_a$  and the measured ones was good with relatively high values of  $r^2$  obtained by linear regression analysis and with slopes and intercepts close to 1 and 0 respectively, as shown in Table 6. This close correspondence demonstrates the broad scale applicability of the equations and coefficients given in Table 3 for the prediction of  $\text{EC}_a$  from  $\text{EM}_H$  and  $\text{EM}_V$ .

Table 2. Comparison of regression  $r^2$  and press statistics values for the linear combination models (Eq. [10] vs. [11]).

Profile	Depth	Data Set	$n$	Model			
				Eq. [10]		Eq. [11]	
				$r^2$	Press Stat	$r^2$	Press Stat
$\text{EM}_H \leq \text{EM}_V$	0–30	A	300	0.613	5.379	0.724	3.871
		B	372	0.545	8.592	0.739	4.930
	30–60	A	360	0.723	5.719	0.773	4.695
		B	287	0.719	7.044	0.790	5.260
	60–90	A	92	0.711	1.561	0.708	1.578
		B	114	0.747	2.049	0.753	2.002
$\text{EM}_H > \text{EM}_V$	0–30	A	60	0.787	1.032	0.860	0.669
		B	56	0.864	0.730	0.875	0.672
	30–60	A	59	0.824	0.785	0.824	0.785
		B	53	0.850	0.747	0.855	0.747
	60–90	A	26	0.777	0.460	0.763	0.489
		B	20	0.842	0.409	0.870	0.337

Table 3. Relations found between soil electrical conductivity in the different soil depth increments and the electromagnetic measurements made with the EM-38 device, where  $\text{EC}_a$  was measured with the Martek SCT insertion probe.

Depth, cm	Equations for electrical conductivity†	$n$	$r^2$
for $\text{EM}_H \leq \text{EM}_V$			
0–30	$\text{EC}_a^{\hat{}} = 3.023 \text{EM}_H^{\hat{}} - 1.982 \text{EM}_V^{\hat{}}$	673	0.731
0–60	$\text{EC}_a^{\hat{}} = 2.757 \text{EM}_H^{\hat{}} - 1.539 \text{EM}_V^{\hat{}} - 0.097$	639	0.835
0–90	$\text{EC}_a^{\hat{}} = 2.028 \text{EM}_H^{\hat{}} - 0.887 \text{EM}_V^{\hat{}}$	198	0.852
30–60	$\text{EC}_a^{\hat{}} = 2.585 \text{EM}_H^{\hat{}} - 1.213 \text{EM}_V^{\hat{}} - 0.204$	647	0.782
60–90	$\text{EC}_a^{\hat{}} = 0.958 \text{EM}_H^{\hat{}} + 0.323 \text{EM}_V^{\hat{}} - 0.142$	195	0.736
for $\text{EM}_H > \text{EM}_V$			
0–30	$\text{EC}_a^{\hat{}} = 1.690 \text{EM}_H^{\hat{}} - 0.591 \text{EM}_V^{\hat{}}$	117	0.866
0–60	$\text{EC}_a^{\hat{}} = 1.209 \text{EM}_H^{\hat{}} - 0.089$	147	0.917
0–90	$\text{EC}_a^{\hat{}} = 1.107 \text{EM}_H^{\hat{}}$	54	0.903
30–60	$\text{EC}_a^{\hat{}} = 0.554 \text{EM}_H^{\hat{}} + 0.595 \text{EM}_V^{\hat{}}$	113	0.840
60–90	$\text{EC}_a^{\hat{}} = -0.126 \text{EM}_H^{\hat{}} + 1.283 \text{EM}_V^{\hat{}} - 0.097$	53	0.812

†  $\text{EC}_a^{\hat{}}$ ,  $\text{EM}_H^{\hat{}}$  and  $\text{EM}_V^{\hat{}}$  are the fourth roots of  $\text{EC}_a$ ,  $\text{EM}_H$  and  $\text{EM}_V$ .

The Wenner data was also tested for parameter stability, using the following relation

$$EC_{a,x1-x2} = B_0 + B_1 (EM_H + EM_V) + B_2 (DS). [12]$$

The values of  $B_2$  were not significantly different from zero in any case (see Table 4); thus, parameter convergence was obtained using Eq. [12]. Since collinearity was not a problem and parameter stability was obtained with the two Wenner split data sets, a comparison between  $EM_H$ ,  $EM_V$  and  $EC_a$  values was made by multilinear regression analysis using the combined data set. Results are given in Table 5. The larger  $r^2$  values obtained with the Wenner method of measuring  $EC_a$  compared to the Martek SCT method are most likely due to differences in the two instrument's sampling volumes. The sample volumes for the Wenner and EM methods are similar, while the volume sampled by the SCT is much smaller.

The equations given in Table 5 were used to predict  $EC_a$  values from given  $EM_H$  and  $EM_V$  values. The

predicted values compared well with the actual values of  $EC_a$  (Table 6).

To compare the new relations established herein with those previously obtained by Corwin and Rhoades (1982, 1983), linear regression analyses were performed between the measured and predicted values of  $EC_a$  in the 0- to 30- and 30- to 60-cm depths. For this purpose the Martek SCT coefficients of Table 3 were used, since this method of measurement was common to both studies. The new relations consistently give slopes and intercepts closer to 1.0 and 0.0, respectively, and frequently higher  $r^2$  values (see Table 7). The values of  $r^2$  are generally good.

The highly sampled data set (consisting of 18 sites) was used to evaluate the accuracy of the  $EC_a$  values predicted from  $EM_H$  and  $EM_V$  using the values of  $k_H$  and  $k_V$  established with the extensive data set. The data and results are given in Tables 8 and 9; predicted

Table 4. Values of  $B_2$  coefficients in Eq. [12] and their  $F$  probability levels, using Wenner values of  $EC_a$ \*\*

Profile	Depth, cm	$B_2$	Pr < $F$
$EM_H \leq EM_V$	0-30	-0.004	0.517
	0-60	-0.000	0.967
	30-60	0.001	0.911
$EM_H > EM_V$	0-30	-0.005	0.647
	0-60	-0.004	0.561
	30-60	0.002	0.853

\*\* Probabilities greater than 0.01 were not considered to be significantly different from zero.

Table 5. The relations between soil electrical conductivity ( $EC_a$ ) as measured by the Wenner array and electromagnetic (EM) measurements made with the EM-38 device.

Depth, cm	Equations for electrical conductivity†	$n$	$r^2$
for $EM_H \leq EM_V$			
0-30	$EC_a = 2.539 EM_H - 1.413 EM_V - 0.068$	759	0.810
0-60	$EC_a = 2.092 EM_H - 0.81 EM_V - 0.179$	761	0.895
30-60	$EC_a = 1.894 EM_H - 0.407 EM_V - 0.292$	758	0.840
for $EM_H > EM_V$			
0-30	$EC_a = 1.164 EM_H - 0.078 EM_V$	165	0.922
0-60	$EC_a = 0.640 EM_H + 0.568 EM_V - 0.114$	163	0.969
30-60	$EC_a = 1.367 EM_V - 0.209$	162	0.919

†  $EC_a$ ,  $EM_H$  and  $EM_V$  are the fourth roots of  $EC_a$ ,  $EM_H$  and  $EM_V$ .

Table 6. Results of linear regression between predicted (Tables 3 and 5) and measured values of  $EC_a$  by soil depth interval, profile condition and method of measurement of  $EC_a$  (SCT vs. Wenner).

Depth, cm	SCT method				Wenner method			
	$n$	Slope	Intercept	$r^2$	$n$	Slope	Intercept	$r^2$
for $EM_H \leq EM_V$								
0-30	698	1.088	+0.011	0.702	784	1.065	-0.007	0.812
0-60	663	0.965	+0.102**	0.854	786	1.042	+0.016	0.875
0-90	206	1.031	-0.013	0.854	—	—	—	—
30-60	671	0.922	+0.220**	0.801	782	1.040	+0.022	0.807
60-90	216	0.953	+0.168	0.751	—	—	—	—
for $EM_H > EM_V$								
0-30	88	1.149	-0.218	0.857	101	1.179	-0.138**	0.924
0-60	85	1.019	+0.060	0.899	99	1.101	-0.048**	0.968
0-90	30	1.057	+0.066	0.830	—	—	—	—
30-60	85	1.099	-0.048	0.851	99	1.099	-0.049	0.926
60-90	32	1.275	-0.112	0.816	—	—	—	—

\*\* Intercept is significant at the 0.01 alpha level.

Table 7. Comparison of measured  $EC_a$  values with those predicted by new and previous relations.†

Relation‡	Profile	Depth, cm	$n$	Slope	Int	$r^2$
New	$EM_H > EM_V$	0-30	88	1.15	-0.22	0.86
Previous	$EM_H > EM_V$	0-30	88	1.41	-0.45	0.86
New	$EM_H > EM_V$	30-60	85	1.10	-0.05	0.85
Previous	$EM_H > EM_V$	30-60	85	2.77	-1.32	0.67
New	$EM_H > EM_V$	60-90	32	1.28	-0.11	0.82
Previous	$EM_H > EM_V$	60-90	32	1.51	-0.10	0.71
New	$EM_H > EM_V$	0-60	85	1.02	0.06	0.90
Previous	$EM_H > EM_V$	0-60	85	1.76	-0.54	0.84
New	$EM_H > EM_V$	0-90	30	1.06	0.07	0.83
Previous	$EM_H > EM_V$	0-90	30	1.80	-0.47	0.79
New	$EM_H \leq EM_V$	0-30	698	1.09	0.01	0.70
Previous	$EM_H \leq EM_V$	0-30	698	1.29	-0.13	0.61
New	$EM_H \leq EM_V$	30-60	671	0.92	0.22	0.80
Previous	$EM_H \leq EM_V$	30-60	671	1.39	0.45	0.80
New	$EM_H \leq EM_V$	60-90	216	0.95	0.17	0.75
Previous	$EM_H \leq EM_V$	60-90	216	0.57	1.24	0.72
New	$EM_H \leq EM_V$	0-60	663	0.96	0.10	0.85
Previous	$EM_H \leq EM_V$	0-60	663	1.44	0.07	0.85
New	$EM_H \leq EM_V$	0-90	206	1.03	-0.01	0.85
Previous	$EM_H \leq EM_V$	0-90	206	0.89	0.62	0.86
New	$EM_H > EM_V$	0-30, & 30-60 & 60-90	1790	0.99	0.11	0.80
Previous	$EM_H > EM_V$	0-30, & 30-60 & 60-90	1790	0.98	0.56	0.61

† Measured  $EC_a$  = (slope) predicted  $EC_a$  ± intercept;  $n$  = number of samples;  $r^2$  = coefficient of determination.

‡  $EC_a$  values measured with four-electrode insertion probe (Rhoades and van Schilfgaarde, 1976) and values predicted using relations developed herein (Table 3) and those of Corwin and Rhoades (1982, 1983).

Table 8. Measured values of  $EM_H$ ,  $EM_V$  and  $EC_a$  and predicted values of  $EC_a$  to small, well-sampled data set.

Site number	Measured, dS/m					Predicted $EC_a$ , dS/m		
	EM		$EC_a$			0-30†	30-60	60-90
	H	V	0-30†	30-60	60-90			
1	4.30(0.08)‡	3.49(0.04)	7.1 (0.3)	4.5 (0.3)	4.5 (0.5)	7.0	6.7	4.7
2	0.73(0.01)	0.83(0.00)	0.72(0.03)	0.49(0.07)	1.21(0.05)	0.66	1.1	1.22
3	0.80(0.00)	0.78(0.00)	0.94(0.04)	0.94(0.02)	1.13(0.02)	0.98	1.5	1.30
4	2.40(0.02)	2.18(0.01)	3.5 (0.3)	2.9 (0.2)	2.2 (0.1)	3.7	4.0	2.9
5	0.36(0.00)	0.42(0.00)	0.39(0.03)	0.26(0.02)	0.50(0.05)	0.31	0.46	0.55
6	1.21(0.01)	1.04(0.01)	1.29(0.06)	0.68(0.05)	0.78(0.06)	1.9	1.9	1.29
7	0.42(0.00)	0.59(0.00)	0.18(0.01)§	0.17(0.02)§	—¶	0.23	0.44	—¶
8	1.77(0.04)	1.48(0.03)	3.4 (0.1)	1.3 (0.1)	0.44(0.04)	2.8	2.8	1.9
9	0.41(0.00)	0.16(0.00)	1.25(0.08)	—¶	—¶	0.92	—¶	—¶
10	1.13(0.01)	1.11(0.01)	1.32(0.07)	1.65(0.06)	2.09(0.08)	1.37	2.19	1.92
11	2.79(0.03)	1.83(0.04)	5.1 (0.1)	4.5 (0.1)	2.31(0.08)	5.0	3.9	2.31
12	0.68(0.01)	0.76(0.00)	0.56(0.04)	1.02(0.05)	1.00(0.04)	0.62	1.03	1.13
13	1.09(0.01)	1.27(0.01)	0.64(0.05)	1.37(0.08)	1.69(0.06)	0.94	1.74	1.94
14	3.30(0.08)	2.79(0.07)	5.9 (0.3)	5.1 (0.2)	2.6 (0.1)	5.2	5.3	3.7
15	0.53(0.01)	0.52(0.00)	0.55(0.03)	0.82(0.04)	0.91(0.01)	0.64	0.89	0.81
16	1.70(0.02)	1.45(0.01)	2.65(0.08)	1.7 (0.1)	1.67(0.07)	2.7	2.7	1.85
17	1.08(0.02)	1.11(0.01)	1.16(0.08)	2.22(0.04)	1.24(0.03)	1.20	2.0	1.85
18	2.58(0.05)	1.86(0.04)	3.3 (0.2)	2.5 (0.1)	1.5 (0.1)	4.4	3.8	2.4

† Soil depth interval, centimeters.

‡ ( ) = Standard error of mean.

§  $n = 6$  instead of 8 as for all other sites.

¶ Unable to insert SCT into this soil depth interval.

Table 9. Results of linear regression between predicted (from coefficients of Table 3) and measured values of  $EC_a$  for a small, well-sampled data set (Table 8).†

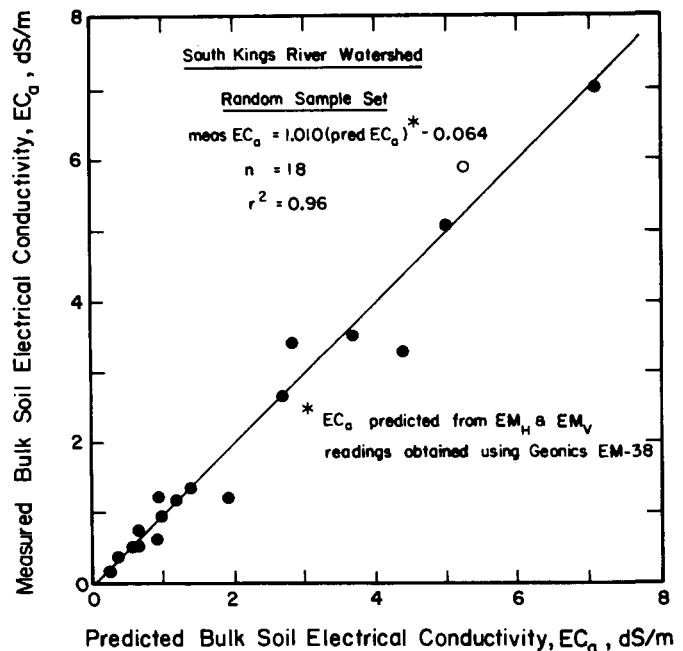
Soil depth, cm	$n$	$r^2$	Slope	Intercept
For $EM_H \leq EM_V$				
0-30	9	0.92	0.91(0.10)‡	0.01(0.09)
30-60	8	0.82	0.96(0.17)	-0.21(0.24)
60-90	8	0.79	0.82(0.17)	0.11(0.25)
For $EM_H > EM_V$				
0-30	9	0.92	1.01(0.11)	-0.07(0.47)
30-60	8	0.74	0.93(0.22)	-0.70(0.93)
60-90	8	0.84	1.03(0.18)	-0.71(0.51)
For both profile types				
0-30	18	0.96	1.01(0.05)	-0.06(0.15)
30-60	16	0.84	0.81(0.09)	-0.13(0.27)
60-90	16	0.82	0.84(0.11)	-0.06(0.24)

† Measured  $EC_a = (\text{slope}) \text{ predicted } EC_a \pm \text{intercept}$ ;  $n$  = number of samples;  $r^2$  = coefficient of determination.

‡ Values within ( ) are standard errors.

and measured  $EC_a$  values for one depth (0-30 cm) are given in Fig. 1 to facilitate the visualization of the degree of correspondence obtained. Higher  $r^2$  values between predicted and measured values of  $EC_a$  were obtained in this more accurate data set, especially in the 0- to 30-cm soil-depth interval, compared to the major data set. The better relationship is attributed to the multiple Martek SCT measurements that were made in the acquisition of these data, which gives a closer approximation of the mean  $EC_a$  value of the relatively large soil volume sensed by the Geonics EM-38.

Predicted and measured  $EC_a$  values often differed considerably from the  $EM_H$  and  $EM_V$  values per se (see Table 8). The closer correspondence existing between measured and predicted  $EC_a$  values than between measured  $EC_a$  and  $EM_H$  and  $EM_V$  values shown in these data clearly demonstrates the advantage of using the predictions of  $EC_a$  from  $EM_H$  and  $EM_V$  in lieu of the values of  $EM_H$  and  $EM_V$  per se for the purpose of salinity appraisal. Even though the predictions are not as accurate as desired in the 30- to 60-

Fig. 1. Correspondence between measured and predicted soil electrical conductivities ( $EC_a$ ) for a random sample set of soils from the South Kings River Watershed, 0 to 30-cm depth.

and 60- to 90-cm depths, they are still reasonable estimates that should provide more meaningful information with which to interpret soil salinity within the plant root zone than the EM values themselves.

## CONCLUSION

The equations given in Tables 3 and 5 yield estimates of  $EC_a$  within the soil-depth intervals of 0 to 30, 30 to 60 or 60 to 90 cm from  $EM_H$  and  $EM_V$  measurements that should be more generally applicable than those previously given in Corwin and Rhoades (1982, 1983), since they are based on a more extensive data set and have been developed using statistical

techniques designed to combat the inherent interdependence between the  $EM_H$  and  $EM_V$  measurements.

### REFERENCES

- Corwin, D.L., and J.D. Rhoades. 1982. An improved technique for determining soil electrical conductivity—depth relations from above ground electromagnetic measurements. *Soil Sci. Soc. Am. J.* 46:517–520.
- Corwin, D.L., and J.D. Rhoades. 1983. Measurement of inverted electrical conductivity profiles using electromagnetic induction. *Soil Sci. Soc. Am. J.* 48:288–291.
- Davis, John C. 1986. Principal components analysis. p. 527–546. *In* Statistical and data analysis in geology, 2nd Ed. Kansas geological survey. John Wiley & Sons, Inc., New York.
- Myers, Raymond H. 1986. Press statistics, p. 100–136; and Detecting and combating multicollinearity, p. 243–263. *In* Classical and modern regression with applications. Duxberg Press, Boston Mass.
- Rhoades, J.D. 1976. Measuring, mapping and monitoring field salinity and water table depths with soil resistance measurements. *FAO Soils Bull.* 31:69–109.
- Rhoades, J.D., and D.L. Corwin. 1981. Determining soil electrical conductivity—depth relations using an inductive electromagnetic soil conductivity meter. *Soil Sci. Soc. Am. J.* 45:255–260.
- Rhoades, J.D., and J. van Schilfgaarde. 1976. An electrical conductivity probe for determining soil salinity. *Soil Sci. Soc. Am. J.* 40:647–651.
- SAS Institute, Inc. 1985. SAS/STAT procedures guide for personal computers, 6th ed. SAS Inst. Inc., Gary, NC.
- Shapiro, S.S., and M.B. Wilk. 1965. An analysis of variance test for normality (complete samples). *Biometrika* 52:591–611.
- Statgraphics. 1986. Regression analyses. p. 1–47. *In* Statistical graphics system. Statistical Graphics Corporation, Rockville, MD.
- Tukey, J.W. 1977. Stem and leaf analysis. p. 1–26. *In* Exploratory data analysis. Addison-Wesley, Reading, MA.